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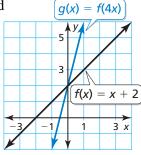
Chapter 1 (p. 30)

*Chapter 1 (p. 4)* 

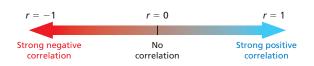
A transformation that causes the graph of a function to shrink toward the y-axis when all the x-coordinates are multiplied g(x) = f(4x)

by a factor a, where a > 1

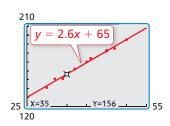
The graph of g is a horizontal shrink of the graph of f by a factor of  $\frac{1}{4}$ .



A number r form -1 to 1 that measures how well a line fits a set of data pairs (x, y)



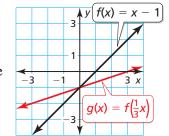
A line that lies as close as possible to all of the data points in a scatter plot



A transformation that causes the graph of a function to stretch away from the *y*-axis when all the *x*-coordinates are multiplied by a factor *a*,

where 
$$0 < a < 1$$

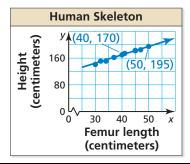
The graph of g is a horizontal stretch of the graph of f by a factor of  $1 \div \frac{1}{3} = 3$ .



An equation of the form ax + by + cz = d, where x, y, and z are variables and a, b, and c are not all zero

$$2x - 5y + 6z = 1$$

A line that models data in a scatter plot



The most basic function in a family of functions

The parent function of absolute value functions is f(x) = |x|.

A solution of a system of three linear equations represented by (x, y, z)

$$(-1, 2, 5)$$

Vocabulary Flash Cards	
reflection	solution of a system of three linear equations
Chapter 1 (p. 5)	Chapter 1 (p. 30)
system of three linear equations	transformation
Chapter 1 (p. 30)	Chapter 1 (p. 5)
translation  Chapter 1 (p. 5)	vertical shrink  Chapter 1 (p. 6)
vertical stretch  Chapter 1 (p. 6)	

An ordered triple (x, y, z) whose coordinates make each equation true

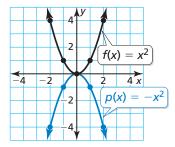
$$4x + 2y + 3z = 12$$
 Equation 1

$$2x - 3y + 5z = -7$$
 Equation 2

$$6x - y + 4z = -3$$
 Equation 3

A transformation that flips a graph over the line of reflection

The graph of p(x) is a reflection in the *x*-axis of the parent quadratic function.



A change in the size, shape, position, or orientation of a graph

See translation, reflection, horizontal shrink, horizontal stretch, vertical shrink, and vertical stretch.

A set of three equations of the form ax + by + cz = d, where x, y, and z are variables and a, b, and c are not all zero

$$3x + 4y - 8z = -3$$
 Equation 1

$$x + y + 5z = -12$$
 Equation 2

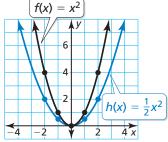
$$4x - 2y + z = 10$$
 Equation 3

A transformation that causes the graph of a function to shrink toward the *x*-axis when all the *y*-coordinates are multiplied by a factor *a*, where

0 < a < 1

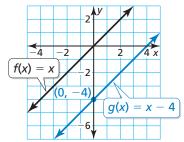
The graph of  $g(x) = \frac{1}{2}x^2$  is a

vertical shrink of the graph of the parent quadratic function.



A transformation that shifts a graph horizontally and/or vertically but does not change its size, shape, or orientation

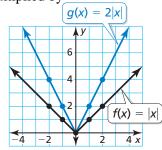
The graph of g(x) = x - 4 is a vertical translation 4 units down of the graph of the parent linear function.



A transformation that causes the graph of a function to stretch away from the *x*-axis when all the *y*-coordinates are multiplied by

a factor a, where a > 1

The graph of g(x) = 2|x| is a vertical stretch of the graph of the parent absolute value function.

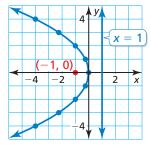


Vocabulary Flash Cards	
axis of symmetry	directrix
Chapter 2 (p. 56)	Chapter 2 (p. 68)
focus	intercept form
Chapter 2 (p. 68)	Chapter 2 (p. 59)
maximum value  Chapter 2 (p. 58)	minimum value  Chapter 2 (p. 58)
parabola	quadratic function
Chapter 2 (p. 48)	Chapter 2 (p. 48)

A fixed line perpendicular to the axis of symmetry such that the set of all points (x, y) of the parabola

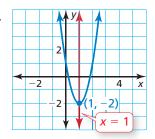
are equidistant from the focus and the directrix

The directrix of  $x = -\frac{1}{4}y^2$  is x = 1.



A line that divides a parabola into mirror images and passes through the vertex

The axis of symmetry of  $f(x) = 3x^2 - 6x + 1$  is x = 1.

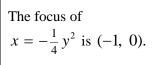


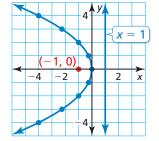
A quadratic function written in the form f(x) = a(x - p)(x - q), where  $a \ne 0$ 

$$f(x) = 2(x-3)(x-1)$$
$$f(x) = 3(x+4)(x-2)$$

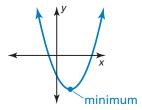
A fixed point in the interior of a parabola, such that the set of all points (x, y) of the parabola are

equidistant from the focus and the directrix

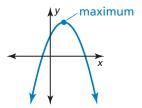




The y-coordinate of the vertex of the quadratic function  $f(x) = ax^2 + bx + c$  when a > 0



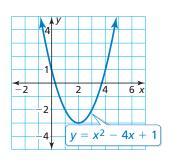
The y-coordinate of the vertex of the quadratic function  $f(x) = ax^2 + bx + c$  when a < 0



A function that can be written in the form  $f(x) = a(x - h)^2 + k$ , where  $a \ne 0$ 

$$f(x) = (x+4)^2 - 1$$

The graph of a quadratic function



Vocabulary Flash Cards	
standard form	vertex form
Chapter 2 (p. 56)	Chapter 2 (p. 50)
vertex of a parabola  Chapter 2 (p. 50)	

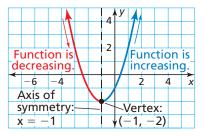
A quadratic function written in the form  $f(x) = a(x - h)^2 + k$ , where  $a \ne 0$ 

$$f(x) = 3(x - 2)^2 + 1$$

A quadratic function written in the form  $f(x) = ax^2 + bx + c$ , where  $a \ne 0$ 

$$f(x) = 2x^2 - x + 3$$

The lowest point on a parabola that opens up or the highest point on a parabola that opens down



Vocabulary Flash Cards	
completing the square	complex number
Chapter 3 (p. 112)	Chapter 3 (p. 104)
discriminant	imaginary number
Chapter 3 (p. 124)	Chapter 3 (p. 104)
imaginary unit <i>i</i>	pure imaginary number
Chapter 3 (p. 104)	Chapter 3 (p. 104)
quadratic equation in one variable	Quadratic Formula
Chapter 3 (p. 94)	Chapter 3 (p. 122)

A number written in the form $a +$	-bi, where $a$ and
b are real numbers	

5 + 2i

To add a term c to an expression of the form  $x^2 + bx$  such that  $x^2 + bx + c$  is a perfect square trinomial

$$x^{2} + 6x + 9 = (x + 3)^{2}$$
  
 $x^{2} + bx + \left(\frac{b}{2}\right)^{2} = \left(x + \frac{b}{2}\right)^{2}$ 

A number written in the form a + bi, where a and b are real numbers and  $b \neq 0$ 

10 - 2i

The expression  $b^2 - 4ac$  in the Quadratic Formula

The value of the discriminant of the equation  $3x^2 - 2x - 7 = 0$  is

$$b^2 - 4ac = (-2)^2 - 4(3)(-7) = 88.$$

A number written in the form a + bi, where a = 0 and  $b \neq 0$ 

5i

The square root of -1, denoted  $i = \sqrt{-1}$ 

$$i = \sqrt{-1}$$

The solutions of the quadratic equation

$$ax^2 + bx + c = 0$$
 are  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

where a, b, and c are real numbers and  $a \neq 0$ .

To solve  $2x^2 + 13x - 7 = 0$ , substitute 2 for a, 13 for b, and -7 for c in the Quadratic Formula.

$$x = \frac{-13 \pm \sqrt{13^2 - 4(2)(-7)}}{2(2)} \rightarrow x = \frac{1}{2} \text{ and } x = -7$$

An equation that can be written in the standard form  $ax^2 + bx + c = 0$ , where a, b, and c are real numbers and  $a \neq 0$ 

$$2x^2 - 3x + 8 = 0$$

An inequality of the form  $y < ax^2 + bx + c$ ,  $y > ax^2 + bx + c$ , or  $y \ge ax^2 + bx + c$ , where a, b, and c are real numbers and  $a \ne 0$ 

$$y < -x^2 - 2x - 1$$

An inequality of the form  $ax^2 + bx + c < 0$ ,  $ax^2 + bx + c > 0$ ,  $ax^2 + bx + c \le 0$ , or  $ax^2 + bx + c \ge 0$ , where a, b, and c are real numbers and  $a \ne 0$ 

$$x^2 - 3x - 4 < 0$$

A system of equations where at least one of the equations is nonlinear

$$y = x^2 + 2x - 4$$
 Equation 1  
 $y = 2x + 5$  Equation 2

A solution of an equation

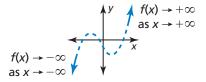
The roots of  $x^2 - x - 6 = 0$  are x = -2 and x = 3.

An x-value of a function f for which f(x) = 0

The zeroes of  $f(x) = x^2 - 4x - 45$  are x = 9 and x = -5.

Vocabulary Flash Cards		
complex conjugates	end behavior	
Chapter 4 (p. 199)	Chapter 4 (p. 159)	
even function	factor by grouping	
Chapter 4 (p. 215)	Chapter 4 (p. 181)	
factored completely	finite differences	
Chapter 4 (p. 180)	Chapter 4 (p. 220)	
local maximum  Chapter 4 (p. 214)	local minimum  Chapter 4 (p. 214)	

The behavior of the graph of a function as x approaches positive infinity or negative infinity



Pairs of complex numbers of the forms a + bi and a - bi, where  $b \neq 0$ 

$$5 + 2i$$
 and  $5 - 2i$ 

A method of factoring a polynomial by grouping pairs of terms that have a common monomial factor

$$t^{3} + t^{2} - 9t - 9 = t^{2}(t+1) - 9(t+1)$$
$$= (t^{2} - 9)(t+1)$$
$$= (t-3)(t+3)(t+1)$$

For a function f, f(-x) = f(x) for all x in its domain

$$f(x) = x^2$$
$$f(x) = 3x^4 - 2x^2$$

The differences of consecutive *y*-values in a data set when the *x*-values are equally spaced

#### Equally-spaced x-values

					$\sim$			_
	X	-3	-2	-1	0	1	2	3
	У	9	4	1	0	1	4	9
first differences: -5 -3 -1 1 3 5						5		

2

2

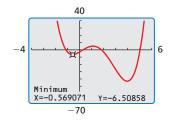
2

2

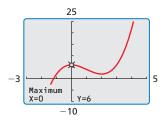
A polynomial written as a product of unfactorable polynomials with integer coefficients

$$x^{3} - 2x^{2} - 8x = x(x^{2} - 2x - 8)$$
$$= x(x - 4)(x + 2)$$

The *y*-coordinate of a turning point of a function when the point is lower than all nearby points



The *y*-coordinate of a turning point of a function when the point is higher than all nearby points



second differences: 2

Vocabulary Flash Cards		
odd function	Pascal's Triangle	
Chapter 4 (p. 215)	Chapter 4 (p. 169)	
polynomial	polynomial function	
Chapter 4 (p. 158)	Chapter 4 (p. 158)	
polynomial long division	quadratic form	
Chapter 4 (p. 174)	Chapter 4 (p. 181)	
repeated solution	synthetic division	
Chapter 4 (p. 190)	Chapter 4 (p. 175)	

A triangular array of numbers such that the numbers in the *n*th row are the coefficients of the terms in the expression of  $(a + b)^n$  for whole number values of n

For a function f, f(-x) = -f(x) for all x in its domain

$$f(x) = x^3$$
$$f(x) = 2x^5 + x^3$$

A function of the form

$$f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$
, where  $a_n \neq 0$ , the exponents are all whole numbers, and the coefficients are all real numbers

$$f(x) = 3x^3 + 4x^2 + 2x - 1$$

A monomial or a sum of monomials

$$5x + 2$$
$$x^2 + 5x + 2$$

An expression of the form  $au^2 + bu + c = 0$ , where u is an algebraic expression

$$16x^4 - 81 = (4x^2)^2 - 81$$
$$= u^2 - 81, \text{ where } u = 4x^2$$

A method to divide a polynomial f(x) by a nonzero divisor d(x) to yield a quotient polynomial q(x) and a remainder polynomial r(x)

$$\begin{array}{r}
x+3 \\
x+1 \overline{\smash)x^2 + 4x + 2} \\
\underline{x^2 + x} \\
3x+2 \\
\underline{3x+3} \\
-1 \\
\underline{x^2 + 4x + 2} \\
x+1 = x+3 - \frac{1}{x+1}
\end{array}$$

A shortcut method to divide a polynomial by a binomial of the form x - k

You can use synthetic division to divide  $x^2 + 4x + 2$  by x + 1.

$$\begin{array}{c|ccccc}
-1 & 1 & 4 & 2 \\
& & -1 & -3 \\
\hline
1 & 3 & -1 & \\
\hline
x^2 + 4x + 2 & = x + 3 - \frac{1}{x+1}
\end{array}$$

A solution of an equation that appears more than once

The equation  $(x + 2)^2 = 0$  has a repeated solution of x = -2.

Vocabulary Flash Cards	
conjugate	extraneous solutions
Chapter 5 (p. 246)	Chapter 5 (p. 263)
index of a radical	inverse functions
Chapter 5 (p. 238)	Chapter 5 (p. 277)
like radicals  Chapter 5 (p. 246)	nth root of a  Chapter 5 (p. 238)
radical equation	radical function
Chapter 5 (p. 262)	Chapter 5 (p. 252)

Solutions that are not solutions of the original
equation

x = -2 is an extraneous solution of  $x + 1 = \sqrt{7x + 15}$  that is introduced by squaring both sides of the equation.

Binomials of the form  $a\sqrt{b}+c\sqrt{d}$  and  $a\sqrt{b}-c\sqrt{d}$ , where a,b,c, and d are rational numbers

$$6\sqrt{5} + 2\sqrt{3}$$
 and  $6\sqrt{5} - 2\sqrt{3}$ 

Functions that undo each other

$$f(x) = 2x - 5$$
 and  $g(x) = \frac{x + 5}{2}$ 

The value of *n* in the radical  $\sqrt[n]{a}$ 

The index of  $\sqrt[3]{70}$  is 3.

For an integer n greater than 1, if  $b^n = a$ , then b is an nth root of a.

$$\sqrt[3]{64} = \sqrt[3]{4 \cdot 4 \cdot 4} = 4$$
  
 $\sqrt[n]{a} = n$ th root of  $a$ 

Radical expressions with the same index and radicand

$$2\sqrt{7}$$
 and  $-3\sqrt{7}$ 

A function that contains a radical expression with the independent variable in the radicand

$$g(x) = -3\sqrt[3]{x}$$

An equation with a radical that has a variable in the radicand

$$2\sqrt{x+1} = 4$$

Vocabulary Flash Cards
simplest form
Chapter 5 (p. 245)

An expression involving a radical with index n that has no radicands with perfect nth powers as factors other than 1, no radicands that contain fractions, and no radicals that appear in the denominator of a fraction

$$\sqrt{27} = 3\sqrt{3}$$

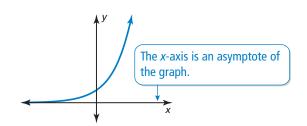
$$\frac{2}{\sqrt{5}} = \frac{2\sqrt{5}}{5}$$

Vocabulary Flash Cards	
asymptote	common logarithm
Chapter 6 (p. 296)	Chapter 6 (p. 311)
decay factor	exponential decay function
Chapter 6 (p. 296)	Chapter 6 (p. 296)
exponential equations	exponential function
Chapter 6 (p. 334)	Chapter 6 (p. 296)
exponential growth function	growth factor
Chapter 6 (p. 296)	Chapter 6 (p. 296)

A logarithm with base 10, denoted as  $\log_{10}$  or simply by  $\log$ 

$$\log_{10} x$$
 or  $\log x$ 

A line that a graph approaches more and more closely



A function of the form  $y = ab^x$ , where a > 0 and 0 < b < 1

$$y = 30(0.75)^x$$

The value of b in an exponential decay function of the form  $y = ab^x$ , where a > 0 and 0 < b < 1

In the exponential decay function  $y = 30(0.75)^x$ , 0.75 is the decay factor.

A function of the form  $y = ab^x$ , where  $a \ne 0$  and the base b is a positive real number other than 1

$$y = 20(0.85)^x$$

Equations in which variable expressions occur as exponents

$$2^x = 7$$
$$5^{x-3} = 25^{x-5}$$

The value of b in an exponential growth function of the form  $y = ab^x$ , where a > 0 and b > 1

In the exponential growth function  $y = 10(1.5)^x$ , 1.5 is the growth factor.

A function of the form  $y = ab^x$ , where a > 0 and b > 1

$$y = 10(1.25)^x$$

Vocabulary Flash Cards	
logarithm of <i>y</i> with base <i>b</i> function	logarithmic equations
Chapter 6 (p. 310)	Chapter 6 (p. 335)
natural base e	natural logarithm
Chapter 6 (p. 304)	Chapter 6 (p. 311)

Equations that involve logarithms of variable expressions	The function $\log_b y = x$ if and only if $b^x = y$ , where $b > 0$ , $y > 0$ , and $b \ne 1$
$\ln(4x - 7) = \ln(x + 5)$	Logarithmic FormExponential Form $log_3 125 = 5$ $5^3 = 125$
A logarithm with base $e$ , denoted by $\log_e$ or $\ln \log_e x = \ln x$	An irrational number approximately equal to $2.71828$ $e \approx 2.71828$

Vocabulary Flash Cards	
complex fraction	constant of variation
Chapter 7 (p. 387)	Chapter 7 (p. 360)
cross multiplying	inverse variation
Chapter 7 (p. 392)	Chapter 7 (p. 360)
rational expression	rational function
Chapter 7 (p. 376)	Chapter 7 (p. 366)
simplified form of a rational expression  Chapter 7 (p. 376)	

The constant a in the inverse variation equation

$$y = \frac{a}{x}$$
, where  $a \neq 0$ 

In the inverse variation equation  $y = \frac{5}{x}$ , 5 is the constant of variation.

A fraction that contains a fraction in its numerator or denominator

$$\frac{\frac{4}{x+3}}{\frac{1}{x+3} + \frac{5}{x}}$$

Two variables *x* and *y* show inverse variation when  $y = \frac{a}{x}$ , where  $a \neq 0$ .

$$y = \frac{2}{x}$$

A method used to solve a rational equation when each side of the equation is a single rational expression

$$\frac{4}{x+1} = \frac{3}{x}$$
$$4x = 3(x+1)$$
$$4x = 3x + 3$$
$$x = 3$$

A function that has the form  $f(x) = \frac{p(x)}{q(x)}$ , where p(x) and q(x) are polynomials and  $q(x) \neq 0$ 

$$g(x) = \frac{4}{x}$$

A fraction whose numerator and denominator are nonzero polynomials

$$\frac{x^2 - 4x - 12}{x^2 - 4}$$

A rational expression whose numerator and denominator have no common factors (other than  $\pm$  1)

$$\frac{15}{65} = \frac{3 \cdot 8}{13 \cdot 8} = \frac{3}{13}$$
$$\frac{4(x+3)}{(x+3)(x+3)} = \frac{4}{x+3}$$

**Vocabulary Flash Cards** arithmetic series arithmetic sequence *Chapter 8 (p. 418) Chapter 8 (p. 420)* common difference common ratio Chapter 8 (p. 418) Chapter 8 (p. 426) explicit rule geometric sequence *Chapter 8 (p. 442) Chapter 8 (p. 426)* geometric series partial sum

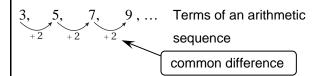
Chapter 8 (p. 428)

*Chapter 8 (p. 436)* 

The expression formed by adding the terms of an arithmetic sequence

$$\sum_{i=1}^{20} (3i + 7)$$

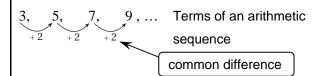
A sequence in which the difference of consecutive terms is constant



The constant ratio r between consecutive terms of a geometric sequence

1, 4, 16, 64, ... Terms of a geometric sequence common ratio

The constant difference d between consecutive terms of an arithmetic sequence



A sequence in which the ratio of any term to the previous term is constant

 $1, \quad 4, \quad 16, \quad 64, \dots \quad \text{Terms of a geometric} \\ \text{sequence} \\ \text{common ratio}$ 

A rule that gives  $a_n$  as a function of the term's position number n in the sequence

$$a_n = 3n - 2$$

The sum  $S_n$  of the first n terms of an infinite series

For the infinite series  $\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \cdots$ , the

first three partial sums are

$$S_1 = \frac{1}{2} = 0.5,$$
  
 $S_2 = \frac{1}{2} + \frac{1}{4} = 0.75,$  and  
 $S_3 = \frac{1}{2} + \frac{1}{4} + \frac{1}{8} = 0.88.$ 

The expression formed by adding the terms of a geometric sequence

$$\sum_{k=1}^{10} 4(3)^{k-1}$$

**Vocabulary Flash Cards** recursive rule sequence Chapter 8 (p. 442) Chapter 8 (p. 410) series sigma notation Chapter 8 (p. 412) *Chapter 8 (p. 412)* 

summation notation terms of a sequence

Chapter 8 (p. 412)

Chapter 8 (p. 410)

An ordered list of numbers

5, 10, 15, 20, ..., 
$$a_n$$
, ...  
2, 4, 8, 16, ...,  $a_n$ , ...

A rule that gives the beginning term(s) of a sequence and a recursive equation that tells how  $a_n$  is related to one or more preceding terms

$$a_0 = 1$$
,  $a_n = a_{n-1} + 4$ 

For any sequence  $a_1, a_2, a_3, \ldots$ , the sum of the first k terms may be written as

$$\sum_{n=1}^{k} a_n = a_1 + a_2 + a_3 + \dots + a_k$$
, where k is an integer.

Finite series: 
$$1 + 3 + 5 + 7 = \sum_{i=1}^{4} 2i - 1$$

Infinite series: 
$$1 + 3 + 5 + 7 + \cdots = \sum_{i=1}^{\infty} 2i - 1$$

The sum of the terms of a sequence

Finite series: 
$$1+3+5+7$$
  
Infinite series:  $1+3+5+7+\cdots$ 

The values in the range of a sequence

5, 10, 15, 20, 25, ..., 
$$a_n$$
, ...

1st position 3rd position  $n$ th position

For any sequence  $a_1, a_2, a_3, \ldots$ , the sum of the first k terms may be written as

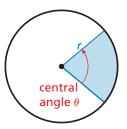
$$\sum_{n=1}^{k} a_n = a_1 + a_2 + a_3 + \dots + a_k$$
, where k is an integer.

Finite series: 
$$1 + 3 + 5 + 7 = \sum_{i=1}^{4} 2i - 1$$

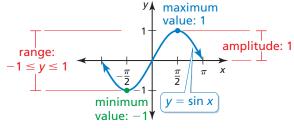
Infinite series: 
$$1 + 3 + 5 + 7 + \cdots = \sum_{i=1}^{\infty} 2i - 1$$

Vocabulary Flash Cards amplitude central angle Chapter 9 (p. 486) Chapter 9 (p. 472) cosine cosecant Chapter 9 (p. 462) Chapter 9 (p. 462) coterminal cotangent *Chapter 9 (p. 462) Chapter 9 (p. 471)* cycle frequency Chapter 9 (p. 486) Chapter 9 (p. 506)

The angle measure of a sector of a circle formed by two radii



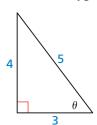
One-half the difference of the maximum value and the minimum value of the graph of a trigonometric function



amplitude = 
$$\frac{1}{2}[1 - (-1)] = 1$$

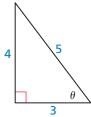
A trigonometric function for an acute angle  $\theta$  of a right triangle, denoted by  $\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$ 

$$\cos\theta = \frac{3}{5}$$

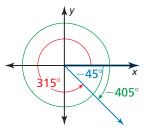


A trigonometric function for an acute angle  $\theta$  of a right triangle, denoted by  $\csc \theta = \frac{\text{hypotenuse}}{\text{opposite}}$ 

$$\csc\theta = \frac{5}{4}$$



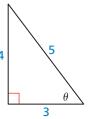
Two angles whose terminal sides coincide



The angles  $315^{\circ}$  and  $-405^{\circ}$  are coterminal with  $-45^{\circ}$ .

A trigonometric function for an acute angle  $\theta$  of a right triangle, denoted by  $\cot \theta = \frac{\text{adjacent}}{\text{opposite}}$ 

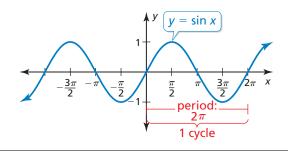
$$\cot \theta = \frac{3}{4}$$



The number of cycles per unit of time, which is the reciprocal of the period

The period of  $\sin 2\pi$  is  $\pi$ , so the frequency is  $\frac{1}{\pi}$ .

The shortest repeating position of the graph of a periodic function



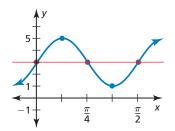
**Vocabulary Flash Cards** initial side midline Chapter 9 (p. 470) Chapter 9 (p. 488) period periodic function Chapter 9 (p. 486) Chapter 9 (p. 486) phase shift quadrantal angle Chapter 9 (p. 488) Chapter 9 (p. 479) radian reference angle Chapter 9 (p. 471) Chapter 9 (p. 480)

The midline of

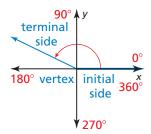
is y = 3.

 $g(x) = 2\sin 4x + 3$ 

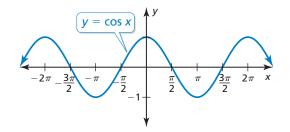
The horizontal line y = k in which the graph of a periodic function oscillates



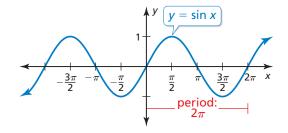
The fixed ray of an angle in standard position in a coordinate plane



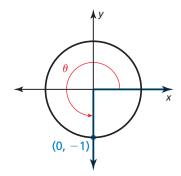
A function whose graph has a repeating pattern



The horizontal length of each cycle of a periodic function



An angle in standard position whose terminal side lies on an axis



A horizontal translation of a periodic function

$$g(x) = a\sin b(x - h) + k$$

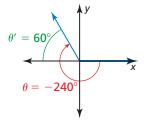
horizontal shift: h

$$g(x) = 5\cos\frac{1}{2}(x - 3\pi)$$

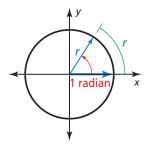
horizontal shift:  $h = 3\pi$ 

The acute angle formed by the terminal side of an angle and the x-axis

The reference angle for 
$$\theta = -240^{\circ}$$
 is  $\theta' = 60^{\circ}$ .

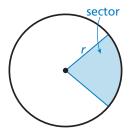


For a circle with radius r, the measure of an angle in standard position whose terminal side intercepts an arc of length r is one radian.



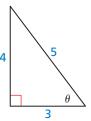
**Vocabulary Flash Cards** sector secant Chapter 9 (p. 462) Chapter 9 (p. 472) sine sinusoid Chapter 9 (p. 507) Chapter 9 (p. 462) standard position tangent *Chapter 9 (p. 470) Chapter 9 (p. 462)* terminal side trigonometric identity Chapter 9 (p. 470) Chapter 9 (p. 514)

A region of a circle that is bounded by two radii and an arc of the circle

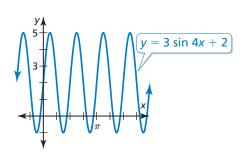


A trigonometric function for an acute angle  $\theta$  of a right triangle, denoted by  $\sec \theta = \frac{\text{hypotenuse}}{\text{adjacent}}$ 

$$\sec \theta = \frac{5}{3}$$

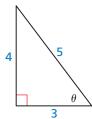


The graph of a sine or cosine function



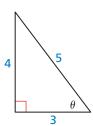
A trigonometric function for an acute angle  $\theta$  of a right triangle, denoted by  $\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$ 

$$\sin\theta = \frac{4}{5}$$

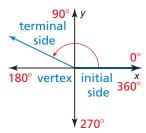


A trigonometric function for an acute angle  $\theta$  of a right triangle, denoted by  $\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$ 

$$\tan\theta = \frac{4}{3}$$



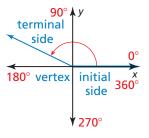
An angle in a coordinate plane such that its vertex is at the origin and its initial side lies on the positive *x*-axis



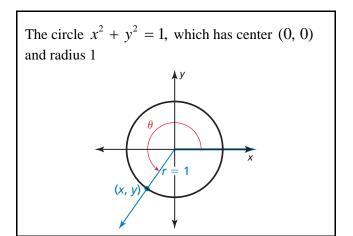
A trigonometric equation that is true for all values of the variable for which both sides of the equation are defined

$$\sin^2 \theta + \cos^2 \theta = 1$$
$$\sin \left(\frac{\pi}{2} - \theta\right) = \cos \theta$$

A ray of an angle in standard position that has been rotated about the vertex in a coordinate plane



Vocabulary Flash Cards
unit circle
Chapter 9 (p. 479)

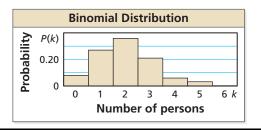


Vocabulary Flash Cards	
binomial distribution	binomial experiment
Chapter 10 (p. 581)	Chapter 10 (p. 581)
Binomial Theorem	combination
Chapter 10 (p. 574)	Chapter 10 (p. 572)
compound event	conditional probability
Chapter 10 (p. 564)	Chapter 10 (p. 547)
conditional relative frequency	dependent events
Chapter 10 (p. 555)	Chapter 10 (p. 547)

An experiment in which there are a fixed number of independent trials, exactly two possible outcomes for each trial, and the probability of success is the dame for each trial

You ask 50 randomly chosen people whether they recycle and 82% responded "yes."

A type of probability distribution that shows the probabilities of the outcomes of a binomial experiment



A selection of objects in which order is not important

The possible combinations of 2 letters chosen from the list A, B, C:

For any positive integer n, the binomial expansion of  $(a + b)^n$  is

$$(a+b)^{n} = {}_{n}C_{0}a^{n}b^{0} + {}_{n}C_{1}a^{n-1}b^{1} + {}_{n}C_{2}a^{n-2}b^{2} + \dots + {}_{n}C_{n}a^{0}b^{n}.$$

$$(x + y^{2})^{3} = {}_{3}C_{0}x^{3}(y^{2})^{0} + {}_{3}C_{1}x^{2}(y^{2})^{1}$$

$$+ {}_{3}C_{2}x^{1}(y^{2})^{2} + {}_{3}C_{3}x^{0}(y^{2})^{3}$$

$$= (1)(x^{3})(1) + (3)(x^{2})(y^{2})$$

$$+ (3)(x^{1})(y^{4}) + (1)(1)(y^{6})$$

$$= x^{3} + 3x^{2}y^{2} + 3xy^{4} + y^{6}$$

The probability that event B occurs given that event A has occurred, written as P(B|A)

the probability of drawing a heart given you drew and did not replace a diamond from a standard deck of 52 cards The union or intersection of two events

selecting a blue marble or a red marble from a bag

Two events in which the occurrence of one event does affect the occurrence of the other event

Randomly selecting a diamond from a standard deck of 52 cards and randomly selecting another diamond from the same deck are dependent events when you do not replace the first card.

The ratio of a joint relative frequency to the marginal relative frequency in a two-way table

		Major in Medical Field		
		Yes	No	
SS	Junior	$\frac{0.18}{0.33} \approx 0.55$	$\frac{0.32}{0.67} \approx 0.48$	<del></del>
Class	Senior	$\frac{0.15}{0.33} \approx 0.45$	$\frac{0.35}{0.67} \approx 0.52$	

Given that a student is not planning to major in a medical field, the conditional relative frequency that he or she is a junior is about 48%.

Vocabulary Flash Cards	
disjoint	event
Chapter 10 (p. 564)	Chapter 10 (p. 538)
experimental probability	geometric probability
Chapter 10 (p. 541)	Chapter 10 (p. 540)
independent events	joint frequency
Chapter 10 (p. 546)	Chapter 10 (p. 554)
ioint relative frequency	marginal frequency
joint relative frequency	marginal frequency
Chapter 10 (p. 555)	Chapter 10 (p. 554)
Спариет 10 (р. 555)	Спаріет 10 (р. 334)

A collection of one or more outcomes in a probability experiment

rolling an odd number when you roll a six-sided die

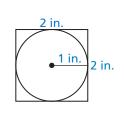
Two events that have no outcomes in common

selecting a diamond or a club from a standard deck of 52 cards

A probability found by calculating a ratio of two lengths, areas, or volumes

The probability that a dart that is equally likely to land anywhere in the square will land in the circle is

$$P(\text{circle}) = \frac{\text{Area of circle}}{\text{Area of square}}$$
$$= \frac{\pi \cdot 1^2}{2^2}$$
$$= \frac{\pi}{4}$$
$$\approx 0.785.$$



The ratio of the number of successes, or favorable outcomes, to the number of trials in a probability experiment

In 100 trials of tossing a coin, the result was heads 56 times and tails 44 times. So, the experimental probability of tossing heads is

$$\frac{56}{100} = 0.56.$$

Each entry in a two-way table

		Student	
		Studied	Did Not Study
Grade	Passed	21	2
Gra	Failed	1	6
joint frequency			

Two events in which the occurrence of one event does not affect the occurrence of another event

selecting a heart from a standard deck of 52 cards and then selecting a red card after replacing the first card

The sums of the rows and columns in a two-way table

		Age			
		12-13	14-15	16-17	Total
Student	Ride Bus	24	12	14	50
Stuc	Does Not Ride Bus	16	13	21	50
	Total	40	25	35/	100
	marginal frequency				

The ratio of a frequency that is not in the total row or the total column to the total number of values or observations in a two-way table

		Major in M		
		Yes	No	Total
Class	Junior	$\frac{124}{680} \approx 0.18$	$\frac{219}{680} \approx 0.32$	0.50
Ü	Senior	$\frac{101}{680} \approx 0.15$	$\frac{236}{680} \approx 0.35$	0.50
	Total /	0.33	0.67	1
joint relative frequency				

Two events that have no outcomes in common

selecting a black card or a red card from a standard deck of 52 cards

The sum of the joint relative frequencies in a row or a column in a two-way table

		Major in M		
		Yes	No	Total
Class	Junior	$\frac{124}{680} \approx 0.18$	$\frac{219}{680} \approx 0.32$	10.50
Ö	Senior	$\frac{101}{680} \approx 0.15$	$\frac{236}{680} \approx 0.35$	0.50
	Total	0.33	_0.67//	<b>1</b>
marginal relative frequency				

The possible result of a probability experiment

The outcomes of flipping a coin are the coin landing heads up or the coin landing tails up.

The product of the integers from 1 to n, for any positive integer n

$$4! = 4 \bullet 3 \bullet 2 \bullet 1 = 24$$

An arrangement of objects in which order is important

The 6 possible permutations of the letters A, B, and C are shown:

ABC ACB BAC BCA CAB CBA

Two events that have one or more outcomes in common

selecting a face card or a diamond from a standard deck of 52 cards

A measure of the likelihood, or chance, that an event will occur

When you roll a six-sided die, the probability of rolling a 4 is  $\frac{1}{6}$ .

A function that gives the probability of each possible value of a random variable

Probability Distribution for Rolling a Six-Sided Die						
X	1	2	3	4	5	6
P(x)	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$

**Vocabulary Flash Cards** probability experiment random variable Chapter 10 (p. 538) Chapter 10 (p. 580) theoretical probability sample space *Chapter 10 (p. 538)* Chapter 10 (p. 539) two-way table Chapter 10 (p. 554)

A variable whose value is determined by the outcomes of a probability experiment

When you roll a six-sided die, you can define a random variable *X* that represents the number showing on the die.

An action, or trial, that has varing results

flipping a coin

The ratio of the number of favorable outcomes to the total number of outcomes when all outcomes are equally likely

You flip a coin. The theoretical probability that the coin lands heads up is

$$P(\text{heads}) = \frac{\text{Number of favorable outcomes}}{\text{Total number of outcomes}} = \frac{1}{2}$$

The set of all possible outcomes for an experiment

The sample space for flipping two coins is listed below.

HH TH HT TT

A frequency table that displays data collected from one source that belong to two different categories

		Fundraiser		
		No	Yes	
Gender	Female	22	51	
Gen	Male	30	29	

Vocabulary Flash Cards	
bias	biased question
Chapter 11 (p. 611)	Chapter 11 (p. 613)
biased sample	cluster sample
Chapter 11 (p. 611)	Chapter 11 (p. 610)
control group	controlled experiment
Chapter 11 (p. 620)	Chapter 11 (p. 620)
convenience sample	descriptive statistics
Chapter 11 (p. 610)	Chapter 11 (p. 626)

A question that is flawed in a way that leads to inaccurate results

The question "Do you agree that we should take a field trip to a science museum this year?" is biased because it encourages a particular response.

An error that results in a misrepresentation of a population

An environmental magazine sends out a survey on recycling to its readers. The sample is biased because the readers of an environmental magazine most likely have a strong opinion about recycling.

A sample in which a population is divided into groups, called clusters, and all of the members in one or more of the clusters are randomly selected

You want to find out whether booth holders at a convention were pleased with their booth locations. You divide the convention center into six sections and survey every booth holder in the fifth section.

A sample that overrepresents or underrepresents part of the population

An environmental magazine sends out a survey on recycling to its readers. The sample is biased because the readers of an environmental magazine most likely have a strong opinion about recycling.

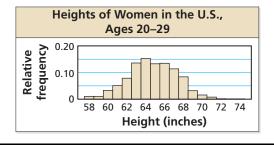
An experiment in which two groups are studied under identical conditions with the exception of one variable

In an experiment studying the effectiveness of a health supplement in aiding weight loss, one group uses a health supplement and another group does not. Both groups exercise regularly and are weighed over a three-month period. The group who does not use the supplement is the control group. The group using the health supplement is the treatment group.

The group under ordinary conditions that is subjected to no treatment during an experiment

In an experiment studying the effectiveness of a health supplement in aiding weight loss, one group uses a health supplement and another group does not. Both groups exercise regularly and are weighed over a three-month period. The group who does not use the supplement is the control group. The group using the health supplement is the treatment group.

The branch of statistics that involves the organization, summarization, and display of data



A sample in which only members of a population that are easy to reach are selected

You are conducting a poll to determine how students feel about your school's new mascot and you only survey the students in your homeroom.

Vocabulary Flash Cards	
experiment	hypothesis
Chapter 11 (p. 612)	Chapter 11 (p. 605)
inferential statistics	information design
Chapter 11 (p. 626)	Chapter 11 (p. 594)
margin of error  Chapter 11 (p. 629)	normal curve Chapter 11 (p. 596)
normal distribution	observational study
Chapter 11 (p. 596)	Chapter 11 (p. 612)

A claim about a characteristic of a population

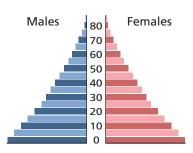
A medical researcher claims that the proportion of U.S. adults living with one or more chronic conditions, such as high blood pressure, is 0.45, or 45%.

A method that imposes a treatment on individuals in order to collect data on their response to the treatment

adding methanol to gasoline and then measuring its effect on fuel efficiency

The designing of data and information so it can be understood and used

The age pyramid shows the ages of males and females in the population of a country.



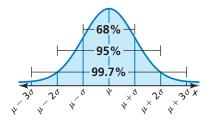
The branch of statistics that involves using a sample to draw conclusions about a population

Two candidates are running for class president. The table shows the results of four surveys of randomly selected students in the class.

Sample Size	Number of "Yes" Responses	Percent of Votes for Incumbent
10	7	70%
20	11	55%
30	13	43.3%
40	17	42.5%

Based on the results of the surveys, you can predict the incumbent will not be reelected.

The graph of a normal distribution that is bell-shaped and is symmetric about the mean



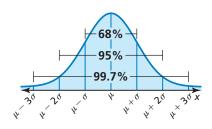
The limit on how much the responses of the sample would differ from the responses of the population

The margin of error of a survey of 1014 people is  $\pm \frac{1}{\sqrt{1014}} \approx 0.031$ , or about 3.1%

Individuals are observed and variables are measured without controlling the individuals or their environment.

A researcher records whether people at a gas station use hand sanitizer.

A type of probability distribution in which the graph is a bell-shaped curve that is symmetric about the mean



Vocabulary Flash Cards		
parameter	placebo	
Chapter 11 (p. 605)	Chapter 11 (p. 620)	
population	random sample	
Chapter 11 (p. 604)	Chapter 11 (p. 610)	
randomization  Chapter 11 (p. 620)	randomized comparative experiment Chapter 11 (p. 620)	
replication	sample	
Chapter 11 (p. 622)	Chapter 11 (p. 604)	

A harmless, unmedicated treatment that resembles the actual treatment

In a study, half the paricipants are given headache medication and the other half are given sugar pills that resemble the headache medication.

A numerical description of a population characteristic

For all students taking the SAT in a recent year, the mean mathematics score was 514.

A sample in which each member of a population has an equal chance of being selected

a survey of 1000 randomly selected adults about how many times per day they brush their teeth

The collection of all data, such as response, measurements, or counts, that you want information about

Population: responses of all adults ages 18 and over in the United States

Sample: 2184 responses of adults in survey

An experiment in which subjects are randomly assigned to the control group or the treatment group

To test the new design of its self checkout, a grocer gathered 142 customers and randomly divided them into two groups. One group used the new self checkout and one group used the old self checkout to buy the same groceries. Users of the new self checkout were able to complete their purchases 16% faster.

A process of randomly assigning subjects to different treatment groups

To test the new design of its self checkout, a grocer gathered 142 customers and randomly divided them into two groups. One group used the new self checkout and one group used the old self checkout to buy the same groceries. Users of the new self checkout were able to complete their purchases 16% faster.

A subset of a population

Population: gasoline mileages of all new cars sold in the United States

Sample: gasoline mileages of 845 new cars in test The repetition of an experiment under the same or similar conditions to improve the validity of the experiment

A lab repeats the same experiment multiple times where participants try a weight loss treatment.

**Vocabulary Flash Cards** simulation self-selected sample Chapter 11 (p. 610) Chapter 11 (p. 612) standard normal distribution statistic Chapter 11 (p. 597) Chapter 11 (p. 605) stratified sample survey Chapter 11 (p. 610) Chapter 11 (p. 612) systematic sample treatment group

# Chapter 11 (p. 610) Chapter 11 (p. 620)

The use of a model to reproduce the conditions of a situation or process so that the simulated outcomes closely match the real-world outcomes  You use a computer program to simulate flipping a coin 10,000 times.	A sample in which members of a population can volunteer to be in the sample  You want to determine whether students in your school like the new design of the school's website. You mail questionnaires and use only the questionnaires that are returned.
A numerical description of a sample characteristic  The mean score on the last exam was 88.	The normal distribution with mean 0 and standard deviation 1  You can use the formula below to transform $x$ -values from a normal distribution with mean $\mu$ and standard deviation $\sigma$ into $z$ -values having a standard normal distribution. $z = \frac{x - \mu}{\sigma}$
An investigation of one or more characteristics of a population  An online poll asks people to select their favorite type of breakfast from a list of options.	A sample in which a population is divided into smaller groups that share a similar characteristic and a sample is then randomly selected from each group  You want to determine whether students in your school like the new design of the school's website. You randomly select two students from each classroom.
The group that is subjected to the treatment in an experiment  In an experiment studying the effectiveness of a health supplement in aiding weight loss, one group uses a health supplement and another group does not. Both groups exercise regularly and are weighed over a three-month period. The group who does not use the supplement is the control group. The group using the health supplement is the treatment group.	A sample in which a rule is used to select members of a population  You want to determine whether students in your school like the new design of the school's website. You list all of the students alphabetically and choose every sixth student.

Vocabulary Flash Cards	
unbiased sample	z-score
Chapter 11 (p. 611)	Chapter 11 (p. 597)

The *z*-score for a particular *x*-value which is the number of standard deviations the *x*-value lies above or below the mean

$$z = \frac{x - \mu}{\sigma}$$

A sample that is representative of the population that you want information about

You randomly select a sample of students from each grade and ask them whether they would rather have a new gymnasium or a new cafeteria.